Fission Cross-Section Measurements of ²⁴⁷Cm, ²⁵⁴Es, and ²⁵⁰Cf from 0.1 eV to 80 keV

Y. Danon, R. E. Slovacek, and R. C. Block

Rensselaer Polytechnic Institute, Department of Nuclear Engineering and Engineering Physics Gaerttner Linac Laboratory, Troy, New York 12180-3590

R. W. Lougheed and R. W. Hoff

Lawrence Livermore National Laboratory, P.O. Box 808, Livermore, California 94550

and

M. S. Moore

Los Alamos National Laboratory, P.O. Box 1663, Los Alamos, New Mexico 87451

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Abstract – The fission cross sections of ²⁴⁷Cm, ²⁵⁴Es, and ²⁵⁰Cf are measured with the Rensselaer intense neutron spectrometer from 0.1 eV to 80 keV. The cross sections are normalized to the ²³⁵U ENDF/B-V broadened cross section. Fission areas and resonance widths are determined for low-energy resonances in ²⁴⁷Cm. The ²⁵⁴Es and ²⁵⁰Cf fission cross sections are the only reported measurements for these isotopes. The ²⁵⁴Es isotope is the heaviest odd-odd isotope ever measured over this energy range. The thermal fission cross sections for ²⁴⁷Cm, ²⁵⁴Es, and ²⁵⁰Cf are determined by extrapolation of the low-energy region of the cross section and are in good agreement with other reported measurements. Resonance integrals are reported for the energy range of 0.1 eV to 80 keV, and the areas for ²⁴⁷Cm and ²⁵⁰Cf resonances are also reported. The previously reported ²⁴⁶Cm fission cross section was corrected for fission in ²⁴⁷Cm.

I. INTRODUCTION

The fission cross sections of the even curium isotopes ²⁴²Cm, ²⁴⁴Cm, ²⁴⁶Cm, and ²⁴⁸Cm were measured at Rensselaer Polytechnic Institute (RPI) previously by Maguire et al. ¹ and Alam et al. ² This measurement completes the fission cross-section measurement set for the curium isotopes.

Einsteinium-254 has a short half-life of 276 days and therefore has a high alpha-particle activity. The fission cross section of such a heavy odd-odd nucleus is interesting for its physical properties, and as is shown, the ²⁵⁴Es fission cross section looks different from all other measurements and shows an interesting lack of structure.

The ²⁵⁰Cf measurement was taken to correct for possible contamination in the einsteinium sample,

which decays by alpha- and beta-particle emission to ²⁵⁰Cf. Because of the high rate of spontaneous fission, this sample had the lowest signal-to-background ratio ever measured in the Rensselaer intense neutron spectrometer (RINS).

The einsteinium, curium, and californium isotopes that were measured are hard to obtain, and only microgram or submicrogram quantities of samples were available; however, the RINS system has the capability to measure such small samples because of its high neutron flux. The RINS system couples the RPI 60-MeV electron linear accelerator (linac) to a lead slowing-down-time spectrometer that consists of a helium-cooled tantalum target inside a 1.8 m on a side, 75-t lead cubic pile. The RINS produces a very intense broad-resolution neutron flux in the energy range of 0.1 to 80 000 eV. The flux intensity obtained is ~10⁴

times greater than an equivalent resolution from a 5-m time-of-flight (TOF) experiment.³ The RINS neutron density has a Gaussian shape with an energy resolution of ~ 0.35 [full-width at half-maximum (FWHM) $\Delta E/E$] from 1 eV to 1 keV.

In order to measure highly alpha-particle active samples, the hemispherical fission chamber was developed⁴ and used in previous RPI RINS measurements of heavy transactinides.^{1,2} The chamber's hemispherical shape combined with very fast rise time custom-designed electronics^{5,6} reduces the alpha-particle pileup problem that might be troublesome otherwise.

II. EXPERIMENTAL METHOD

The RINS system provides an intense source of neutrons with an average neutron energy E (in electron-volts) given by³

$$E = \frac{165\,000}{(t+0.3)^2} \ , \tag{1}$$

where t is the slowing-down time in microseconds. During the linac pulse, the electrons hit the tantalum target and produce intense bremsstrahlung radiation that in turn produces neutrons by a (γ, n) reaction. The pulse of bremsstrahlung, also called gamma flash, causes a high count rate in the fission chamber (due to gamma-induced ionization) and will show up in one of the early channels of the TOF spectrum; this channel is defined as slowing-down-time zero (t = 0). The lead slowing-down-time spectrometer resolution function was first derived theoretically by Bergman et al. 7 Fisher8 made a Monte Carlo calculation with the MCNP code9 and fitted his numerical resolution results to the Bergman et al. theoretical form. The resolution function used by Stopa⁵ and Alam⁶ was used in this work in a resolution-broadening program; the resolution function is given by

$$\left(\frac{dE}{E}\right)_{\text{FWHM}} = \left[0.0835 + \left(\frac{0.128}{E}\right) + 3.05 \times 10^{-5}E\right]^{1/2}$$
 (2)

The relative energy-dependent neutron flux was also fitted by Fisher⁸ and is given by

$$\phi_r(E) = E^{-0.776} \exp\left[-\left(\frac{0.214}{E}\right)^{1/2}\right] ,$$
 (3)

where E represents the average neutron energy as given by Eq. (1). The hemispherical fission chamber used by Alam et al.² and Alam⁶ was used in this experiment; the chamber was filled with 2 atm (absolute) of pure methane gas and was operated with a 500-V negative bias. The sample order in the chamber is shown in Fig. 1. The 235 U + 252 Cf and 252 Cf samples are the

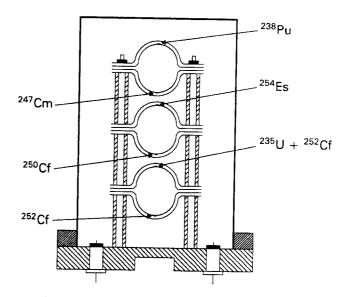


Fig. 1. A side-view sketch of the inside of the fission chamber (not to scale; see Ref. 2 for more details).

same samples used by Alam in his experiment. The 247 Cm, 250 Cf, and 254 Es samples were chemically purified to remove other actinides and any interfering nuclides prior to the measurement. The isotopic content of the samples is listed in Table I. The purified samples were then electroplated as \sim 6-mm-diam spots on the surfaces of hemispherical nickel foils that were assembled in the fission chamber. The electroplating solution was a mixture of 95% isopropyl alcohol and 5% 0.2 N

TABLE I
Sample Contents in the Fission Chamber

Sample	Content	
²⁵² Cf	$313.5 \pm 0.1 \text{ pg}$ (212.01 ± 0.08 fission/s) ^a	
$^{235}U + ^{252}Cf$	$6.37 \mu g^{235} U$ (0.619 ± 0.004 fission/s) ^a	
²⁵⁰ Cf	$0.149 \pm 0.008 \ \mu g$ (441.87 ± 0.11 fission/s) ^a	
²⁵⁴ Es	0.21 \pm 0.01 μ g [13.03 \pm 0.02 fission/s (due to ²⁵⁰ Cf)] ^a	
²⁴⁷ Cm	$3.16 \pm 0.024 \mu g^{247} \text{Cm}$ $3.48 \mu g^{244} \text{Cm}$ $0.093 \mu g^{245} \text{Cm}$ $3.96 \mu g^{246} \text{Cm}$ $0.003 \mu g^{240} \text{Pu}$ $(30.86 \pm 0.03 \text{ fission/s})^a$	

^aThe spontaneous fission count rate of the sample.

HCI. To minimize ²⁵⁰Cf contamination in the einsteinium sample, the ²⁵⁰Cf was separated from the ²⁵⁴Es at Lawrence Livermore National Laboratory (LLNL) 48 h before beginning the collection of data at RPI. The ²⁴⁷Cm is from the same sample used by Moore and Keyworth¹⁰ in their experiment in 1969. The mass content of the ²⁴⁷Cm sample was corrected for isotopic decay. The sample contents are listed in Table I.

Each fission chamber is connected in sequence to a fast preamplifier, a power filter module [both custom designed by Oak Ridge National Laboratory (ORNL) (Ref. 2)], a LeCroy 612M amplifier, and a constant fraction discriminator ORTEC 473A. The constant fraction discriminator was set to a 1.5-V integral discrimination level to discriminate against the lower amplitude alpha-particle signals and electronic noise. The fission detection efficiency was determined by recording the spontaneous fission count rate as a function of discrimination level and by fitting the plateau region to an exponential. The ratio of the count rate at a 1.5-V discrimination level to the extrapolated count rate at zero discrimination is the efficiency η for that sample. The output from each constant fraction discriminator was connected to a TOF clock and an HP-1000, A-900 computer for the data acquisition.

The cylindrical fission chamber was inserted 90 cm deep into the 75-t lead pile in a hole whose axis is 60 cm from the bottom and rear face of the lead cube and was surrounded by machined lead blocks so that there were no big air gaps between the chamber and the lead. The RPI linac was operated at an average current of 15 μ A and an average pulse rate of 90 pulse/s, which gave an average power of 900 W on the tantalum target. The linac pulse width was 200 ns. Data were taken for ~29 h with the linac on and 8 h with the linac off to measure the spontaneous fission background.

III. EXPERIMENTAL DATA REDUCTION

The data were collected in 29 separate files with each file representing a sum of ~1 h of data collecting. The first step was to correct each run for dead time and sum all runs to get one file that contained all the raw data. Since the resolution of the lead spectrometer is relatively broad, the second step was grouping the data into macrochannels with wider time widths than the basic clock channels. The grouping was done in a consistent way with the RINS resolution so that the energy width of the macrochannels did not exceed 25% of the RINS resolution width. The data were reduced from 3072 channels to 150 macrochannels, which gave an improvement of the counting statistics per channel.

The counts in channel i for sample x can be calculated by the following equation:

$$C_i^x = F \cdot \eta^x N^x \phi_r(E_i) \bar{\sigma}_f^x(E_i) \Delta E_i , \qquad (4)$$

where

 C_i^x = counts from sample x in macrochannel i

F =flux normalization factor

 η^x = fission detection efficiency

 N^x = number of atoms of sample x

 E_i = average energy of macrochannel i

 $\phi_r(E_i)$ = relative energy-dependent flux given by Eq. (3)

 $\bar{\sigma}_f^x(E_i)$ = resolution-broadened fission cross section of sample x in channel i

 ΔE_i = channel *i* width in energy units ($\Delta E_i = E_{i+1} - E_i$).

The third step was to find the flux normalization factor relative to ²³⁵U. This was done by first taking the ENDF/B-V (Ref. 11) point cross-section file for ²³⁵U and broadening the cross section with the RINS resolution, ending up with a broadening cross section at average macrochannel energies. The normalization factor is calculated by

$$F = \frac{C_i^{235}}{\eta^{235} N^{235} \phi_r(E_i) \bar{\sigma}_f^{235}(E_i) \Delta E_i} . \tag{5}$$

The term $\bar{\sigma}_f(E_i)$ is the ²³⁵U broadened fission cross section given by

$$\bar{\sigma}_f(E_i) = \frac{1}{\sqrt{E_i}} \int_{E_{min}}^{E_{max}} G(E, E_i) \sqrt{E} \sigma_f(E) dE , \quad (6)$$

where

 $\sigma_f(E) = \text{ENDF/B-V (Ref. 11)}^{235} \text{U fission cross}$ section

 $G(E, E_i)$ = Gaussian resolution function⁶ of the RINS system around energy E_i .

Equation (5) was applied to each channel corresponding to neutron energies from 0.7 to 50 keV. The channel normalization factors were then averaged to give the overall normalization factor F. The standard deviation of the average was taken as the error in F, and this error is 4% over the above normalization energy range. A normalization over all the RINS energy range from 0.1 eV to 100 keV gave a normalization factor that is 5% smaller than the normalization factor used, and this is not a large discrepancy relative to the 10% overall error in the cross section obtained. After F was obtained, the fission cross section of sample x at macrochannel i is given simply by

$$\sigma_f(E_i) = \frac{1}{\eta^x N^x} \frac{C_i^x}{F \phi_r(E_i) \Delta E_i} . \tag{7}$$

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TABLE II Fission Cross Sections and 1σ Error*

1		T		П			,	17			
	²⁴⁷ Cm	²⁵⁴ Es	²⁵⁰ Cf		²⁴⁷ Cm	²⁵⁴ Es	²⁵⁰ Cf	1	²⁴⁷ Cm	²⁵⁴ Es	²⁵⁰ Cf
Energy	σ_f	σ_f	σ_f	Energy	σ_f	σ_f	σ_f	Energy	σ_f	σ_f	σ_f
(eV)	(b)	(b)	(b)	(eV)	(b)	(b)	(b)	(eV)	(b)	(b)	(b)
0.116E+008	<i>EC(C)</i>	755(70)	(0/02)	0.1005		-	 	1	 	 	
0.116E+00 ^a 0.150E+00	56(6)	755(70)	-60(92)	0.192E+02	63(7)	82(8)	3(5)		16(2)	22(2)	0(1)
0.130E+00 0.189E+00	50(6)	698(65)	7(73)	0.205E+02	51(6)	79(7)	9(5)	11	15(2)	21(2)	2(1)
0.189E+00 0.233E+00	45(5) 41(5)	621(58) 574(53)	-22(61)	0.220E+02	40(5)	79(7)	2(4)		15(2)	20(2)	-0.4(0.9)
0.282E+00	39(4)	528(49)	-5(52) 77(46)	0.236E+02 0.254E+02	33(4)	77(7)		0.473E+03	15(2)	18(2)	1(1)
1 1			//(40)	0.234E+02	28(3)	77(7)	1(4)	0.499E+03	15(2)	17(2)	1(1)
0.336E+00	36(4)	495(46)	76(41)	0.270E+02	26(3)	74(7)	3(5)	0.528E+03	15(2)	18(2)	0(1)
0.396E+00	36(4)	449(42)	111(38)	0.284E+02	26(3)	71(7)	5(4)	0.559E+03	14(2)	16(2)	0.0(0.9)
0.461E+00	36(4)	430(40)	169(37)	0.300E+02	25(3)	67(6)	9(4)	0.593E+03	14(2)	16(2)	0.5(0.9)
0.532E+00	38(4)	406(38)	184(35)	0.317E+02	25(3)	67(6)	6(4)		13(1)	16(2)	1.1(0.9)
0.611E+00	47(5)	389(36)	162(32)	0.335E+02	25(3)	62(6)	1(4)	0.672E+03	13(1)	16(2)	1.4(0.8)
0.697E+00	74(8)	350(32)	110(28)	0.355E+02	25(3)	64(6)	3(4)	0.717E+03	12(1)	15(1)	0.4(0.8)
	146(16)	344(32)	99(26)	0.377E+02	26(3)	64(6)	9(4)	0.766E+03	12(1)	15(1)	0.4(0.8) 0.8(0.8)
	285(31)	325(30)	43(23)	0.401E+02	28(3)	61(6)	4(3)	0.821E+03	11(1)	15(1)	0.3(0.7)
	472(51)	314(29)	18(21)	0.427E+02	32(4)	57(5)	3(3)	0.882E+03	11(1)	14(1)	0.3(0.7) 0.1(0.7)
0.112E+01 = 6	625(68)	288(27)	30(20)	0.456E+02	36(4)	59(6)	2(3)	0.951E+03	10(1)	13(1)	0.7(0.6)
0.124E+01 6	647(70)	269(25)	44(19)	0.488E+02	41(5)	58(5)	5(3)	0.103E+04	` ′		
•	539(58)	253(23)	2(18)	0.488E+02 0.523E+02	45(5)	57(5)	4(3)	0.103E+04 0.111E+04	10(1)	13(1)	0.9(0.6)
1	383(41)	240(22)	13(17)	0.562E+02	50(6)	57(5)	2(3)	0.111E+04 0.121E+04	9(1) 9(1)	13(1)	0.6(0.6)
	259(28)	229(21)	27(16)	0.595E+02	53(6)	56(5)	5(4)		9(1)	12(1)	0.6(0.5)
	181(20)	216(20)	-12(15)	0.618E+02	56(6)	55(5)	2(3)	0.127E+04	8.4(0.9)	11(1) 11(1)	-0.3(0.7) -0.1(0.5)
0.202E+01 1	147(16)	202(19)			, ,						
	149(16)	194(18)	10(15)	0.643E+02	57(6)	51(5)	5(3)	0.149E+04	8.1(0.9)	12(1)	0(0)
	191(21)	186(17)	20(14) 6(13)	0.669E+02 0.696E+02	59(7)	52(5)	4(3)	0.162E+04	8.0(0.9)	10(1)	-0.5(0.5)
	258(28)	175(16)	0(13)	0.036E+02 0.726E+02	59(7)	51(5)	2(3)	0.177E+04	7.8(0.9)	11(1)	-0.4(0.4)
·	317(34)	167(16)	28(13)	0.720E+02 0.757E+02	58(6) 55(6)	52(5) 49(5)	6(3) 3(3)	0.193E+04 0.210E+04	7.8(0.9)	10.0(0.9)	-0.4(0.4)
	1				` *	`		0.210E+04	7.6(0.9)	9.4(0.9)	0.0(0.4)
	331(36)	156(15)	-3(11)	0.791E+02	50(6)	47(4)	-1(3)	0.229E+04	7.2(0.8)	9.3(0.9)	-0.1(0.4)
		149(14)	4(11)	0.827E+02	46(5)	46(4)	1(3)	0.251E+04	6.9(0.8)	8.9(0.8)	0.0(0.4)
1		143(13)	8(10)	0.865E+02	41(5)	42(4)	0(3)	0.276E+04	6.6(0.7)	8.5(0.8)	-0.4(0.3)
		136(13) 136(13)	5(10)	0.906E+02	37(4)	42(4)	1(3)	0.304E+04	6.2(0.7)	8.5(0.8)	-0.2(0.3)
	1	130(13)	-12(10)	0.956E+02	34(4)	40(4)	2(2)	0.338E+04	5.9(0.7)	8.0(0.8)	0.4(0.3)
		136(13)	10(10)	0.102E+03	32(4)	38(4)	0(2)	0.374E+04	5.7(0.6)	8.2(0.8)	-0.1(0.3)
		129(12)	8(9)	0.108E+03	29(3)	38(4)	0(2)	0.412E+04	5.5(0.6)	7.5(0.7)	-0.2(0.3)
		128(12)	2(8)	0.115E+03	27(3)	38(4)	1(2)	0.455E+04	5.2(0.6)	7.2(0.7)	0.0(0.3)
		127(12)	9(9)	0.124E+03	25(3)	37(3)	2(2)	0.507E + 04	5.0(0.6)	6.7(0.6)	0.1(0.2)
0.643E+01 1	18(13)	121(11)	7(8)	0.132E+03	23(3)	36(3)	-2(2)	0.567E+04	4.7(0.5)	6.5(0.6)	0.1(0.2)
0.694E+01 1		114(11)	-2(8)	0.142E+03	23(3)	34(3)	0(2)	0.639E+04	4.5(0.5)	6.2(0.6)	-0.1(0.2)
	00(12)	112(10)	7(8)	0.152E+03	23(3)	34(3)	1(2)	0.726E+04	4.2(0.5)	5.8(0.5)	-0.1(0.2) -0.1(0.2)
0.799E+01		106(10)	7(7)	0.162E+03	24(3)	32(3)	1(2)		4.0(0.5)	5.8(0.5)	0.1(0.2)
	92(10)	98(9)	2(7)	0.173E+03	25(3)	30(3)	1(2)	1	3.7(0.4)	5.4(0.5)	0.00(0.10)
0.923E+01	88(10)	91(9)	8(7)	0.184E+03	24(3)	29(3)	2(2)		3.6(0.4)	5.1(0.5)	-0.10(0.10)
0.997E+01	79(9)	87(8)	3(6)	0.197E+03	24(3)	28(3)	ļļ	0.131E+05	3.4(0.4)		
4	69(8)	85(8)	7(7)	0.212E+03	23(3)	28(3)	2(1)		3.4(0.4)	4.7(0.4) 4.5(0.4)	0.00(0.10)
0.114E+02	58(6)	89(8)	-2(6)	0.228E+03	23(3)	27(3)	` ' 11		3.0(0.3)	4.4(0.4)	0.00(0.10)
0.122E+02	49(5)	90(8)	3(6)	0.243E+03	23(3)	26(2)		1	3.0(0.3)	4.2(0.4)	-0.08(0.09)
0.131E+02	43(5)	92(9)	10(6)	0.258E+03	22(2)	26(2)			2.8(0.3)	4.0(0.4)	-0.08(0.09) -0.04(0.08)
0.141E+02	43(5)	88(8)	7(5)	0.274E+03	20(2)					` ′	
	50(6)	92(9)	10(6)	0.274E+03 0.291E+03	19(2)	26(2) 24(2)			2.7(0.3)	3.8(0.4)	0.08(0.07)
	59(7)	90(8)	-2(6)	0.231E+03 0.311E+03	18(2)	24(2)			2.5(0.3)	3.7(0.3)	0.05(0.06)
A 440	67(8)	90(8)	5(5)	0.332E+03	17(2)	23(2)	* ' 11		2.4(0.3) 2.3(0.3)	3.4(0.3)	0.01(0.05)
0.180E+02	69(8)	87(8)		0.355E+03		23(2)	, , 11		2.0(0.2)	3.2(0.3) 3.2(0.3)	0.00(0.04) $-0.04(0.03)$
							-(-/		0(0.2)	3.2(0.3)	0.04(0.03)

^{*}The 1σ error is in parentheses. aRead as 0.116×10^{0} .

IV. RESULTS

The fission cross-section results for ²⁴⁷Cm, ²⁵⁴Es, and ²⁵⁰Cf are listed in Table II and plotted in Figs. 2, 3, and 4. The errors shown in Table II and on Figs. 2, 3, and 4 are due to uncertainties in the fission counting efficiency, the number of atoms in the sample, the neutron flux normalization factor, and the counting statistics. We are able to observe resolved resonances and clusters of resonances below ~200 eV in the ²⁴⁷Cm. At higher energies, the RINS resolution can no longer resolve resonances, and the observed fission cross section is smooth.

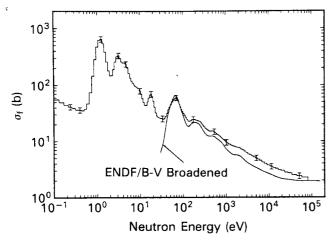


Fig. 2. The ²⁴⁷Cm fission cross section.

IV.A. Curium-247

The ²⁴⁷Cm sample was prepared from the same materials used in Moore and Keyworth's experiment, 10 and this sample contained impurities of mainly ²⁴⁴Cm and ²⁴⁶Cm, as shown in Table I. The fission cross section was corrected for these two isotopes using the results of previous measurements done at RPI by Stopa. 5 The correction was small (<1%) because of the high cross section of ²⁴⁷Cm, relative to ²⁴⁴Cm and ²⁴⁶Cm. In this sample, resonances or clusters of partially resolved resonances were observed up to ~200 eV. The ²⁴⁷Cm cross section reaches a peak of 647 b at 1.2 eV, and resonances were observed at 1.2, 3.1, 4.4, 9.2, and 18.0 eV. At these energies, the only other experimental results available are from the transmission measurement by Belanova et al. 12 They observed five resonances in their data at 1.247, 2.919, 3.189, 9.55, and 18.1 eV. Except for the 4.4-eV resonance, our resonance energies are in good agreement with their energies. The RINS system, however, could not resolve the resonances reported by Belanova et al. at 2.919 and 3.189 eV; we observed only one resonance at 3.1 eV. A resonance was observed at 4.4 eV that was not reported by Belanova et al., and it is possible that this resonance was lost in the corrections that they made for other curium, americium, and plutonium isotopes contained in

To determine the fission widths of the resonances observed, the area under each resonance was determined. The relation between the area under the resonance and the fission width is determined from the Breit-Wigner single-level formula:

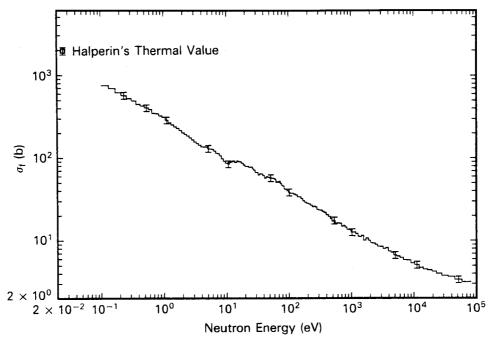


Fig. 3. The ²⁵⁴Es fission cross section.

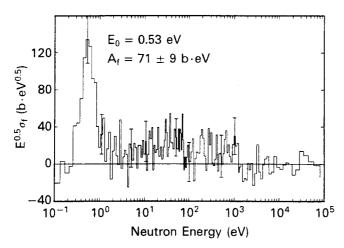


Fig. 4. The ²⁵⁰Cf fission cross section.

$$A_f = \frac{\pi}{2} \sigma_0 \Gamma_f , \qquad (8)$$

where

 A_f = area under the resonance,

$$A_f = \sum \bar{\sigma}(E_i) \Delta E_i$$

 $\bar{\sigma}(E_i)$ = fission cross section in barns at average energy of macrochannel i

 σ_0 = peak cross section in barns given by

$$\sigma_0 = 1.302 \times 10^6 \, \frac{2g\Gamma_n(E_0)}{E_0\Gamma} \ , \qquad (9)$$

where

 E_0 = resonance peak energy (eV)

g = statistical weight factor for s-wave neutrons given by

$$g = \frac{2J+1}{2(2I+1)} \ ,$$

where

I = spin of the nucleus

I = 9/2 for ²⁴⁷Cm and therefore J = 4.5 and $g = 0.5 \pm 0.05$

 $\Gamma, \Gamma_n, \Gamma_f = \text{total}$, neutron, and fission widths, respectively (eV).

The fission widths were calculated using Eq. (8) with the Γ and $2g\Gamma_n$ resonance parameters reported by Belanova et al. ¹² Our results are reported in Table III, where the 1σ errors are due to errors in $\Gamma, 2g\Gamma_n$ reported by Belanova et al., and the error in calculating A_f . The errors in the resonance area A_f were calculated from the overall error in the fission cross section, as reported in Table II. The fission widths of ²⁴⁷Cm were also estimated ¹³ by assuming $\Gamma_{\gamma} = 40$ meV and then $\Gamma_f(E) = \Gamma(E) - \Gamma_n(E) - \Gamma_{\gamma}(E)$; these results are also listed in Table III. A comparison of the two values shows very good agreement; the errors in the fission widths reported are mainly due to errors in the total width Γ as reported by Belanova et al.

Moore and Keyworth¹⁰ measured the ²⁴⁷Cm fission cross section directly by a nuclear explosion experiment, and their results are reported only for energies >20 eV; the resolution of their experiment is much better than the RINS resolution. The Moore and Keyworth fission cross section was broadened to the RINS resolution and plotted in Fig. 2. It is seen that both experiments agree on the shape of the cross section, but the Moore and Keyworth cross section is \sim 30% lower above 150 eV; the source of this discrepancy is unknown.

The fission cross-section low-energy tail was extrapolated to 0.025 eV, and a thermal fission of 106 ± 53 b was obtained for ²⁴⁷Cm. This value agrees with

TABLE III

Resonance Parameters for ²⁴⁷Cm in the Energy Range from 0.1 to 18.1 eV

Belanova et al. 12,a,b			Mughabghab ^{13,c}	This Experiment ^b			
E (eV)	Γ (meV)	$2g\Gamma_n$ (meV)	Γ_f (meV)	Γ _/ (meV)	A_f (b·eV)	E (eV)	
1.247 2.919 3.189 9.55 18.1	$74 \pm 4 70 \pm 30 130 \pm 6 166 \pm 60 210 \pm 170$	$0.56 \pm 0.09 \\ 0.1 \pm 0.04 \\ 1.0 \pm 0.1 \\ \\ 0.9 \pm 0.33 \\ 3.7 \pm 1.5$	$ 34 \pm 7 30 \pm 30 62 \pm 6 125 \pm 60 167 \pm 170 $	34 ± 6 $$ 70 ± 14 $$ 117 ± 83 166 ± 152	427 ± 24 444 ± 70 107 ± 47 141 ± 70 332 ± 46	1.2 3.1 4.4 9.2 18.0	

^aResonance at 4.4 eV was not observed by Belanova et al.

^bResonances reported by Belanova et al. at 2.919 and 3.189 eV, observed in our experiment only as one resonance at 3.1 eV.

[°]Mughabghab¹³ assumes Γ_{γ} = 40 meV and using Γ and Γ_{n} calculates Γ_{f} .

the Mughabghab-evaluated value¹³ of 81.9 ± 4.1 b. The resonance integral from 0.1 eV to 80 keV was also calculated and found to be $I_f = 890 \pm 53$ b, which is slightly higher than the evaluated value¹³ of 760 ± 50 b. Other experimental results are presented in Table IV. The 6% error in the resonance integral is mainly the result of uncertainties in flux normalization, counting efficiency, and sample mass.

The ²⁴⁶Cm fission cross section reported by Maguire et al. ¹ has a resonance at 1.2 eV that was tentatively assigned to ²⁴⁶Cm. Using the ²⁴⁷Cm fission cross section measured in this experiment, we corrected the Maguire et al. measurement for the 0.084% ²⁴⁷Cm impurity in their ²⁴⁶Cm sample. The results of this correction are shown in Fig. 5, where it is seen that the 1.2-eV resonance that appeared in the ²⁴⁶Cm measurement came from the 648-b resonance at 1.2 eV in ²⁴⁷Cm.

The other fission cross sections of even curium isotopes measured at RPI previously^{1,2} did not have any significant correction because of ²⁴⁷Cm impurities in their samples.

IV.B. Einsteinium-254

The 254 Es sample is a pure sample with contamination only from the decay daughters of 254 Es, that is, 250 Bk and 250 Cf. The 250 Bk content in the sample is constant and was calculated to be ~ 0.04 wt%, which

would have negligible effects on the fission cross section of ²⁵⁴Es. The ²⁵⁰Cf was growing into the sample during the measurement. When the experiment started ~48 h after the separation of ²⁵⁰Cf and ²⁵⁰Bk from the ²⁵⁴Es at LLNL, we measured, by counting the spontaneous fission background, ~1 wt% of ²⁵⁰Cf in the sample. At the end of the experiment, ~81 h later, we measured 2 wt% of ²⁵⁰Cf in the sample. The effect of this ²⁵⁰Cf buildup on the cross section is negligible because of the very low fission cross section of ²⁵⁰Cf. The spontaneous fission of the ²⁵⁰Cf was subtracted as a constant background counting rate.

The ²⁵⁴Es fission cross section plotted in Fig. 3 shows very unusual structure. The cross section is decreasing as a function of energy in a rather smooth way with only some structure observed around 4.3 and 13.1 eV; the cross section seems to behave like 1/v up to 10 eV, and above 10 eV, it is falling slower than 1/v. There are two possible explanations for not observing any structure in our measurement. As an odd-odd nucleus, the level spacing of ²⁵⁴Es was calculated by Diamond et al. 15 using the Gilbert and Cameron 23 approach to be 1.1 eV. We calculated a level spacing of 0.9 eV using the Gilbert and Cameron approach assuming a binding energy of 6.26 MeV (calculated from the mass of ²⁵⁴Es, ²⁵⁵Es, and the neutron mass), a deformed nucleus model, and calculating the rest of the parameters (a and σ) from data given by Gilbert and Cameron; it is possible that the level spacing is even

TABLE IV		
Thermal Fission Cross Section and Resonance Integrals* for ²⁵⁴ Es, ²	²⁴⁷ Cm, a	and ²⁵⁰ Cf

Sample	References	σ_f (0.025 eV) (b)	I_f (b)
²⁵⁴ Es	Diamond et al. 15	3060 ± 180	
	MacMurdo and Harbour ¹⁶	2930 ± 130	2200 ± 90
	Halperin et al. 17	1970 ± 200	1200 ± 250
	This Experiment	1749 ± 110	896 ± 54
²⁴⁷ Cm	Ice ¹⁸	1400	
	Diamond et al. 15	108 ± 5	
	Smith et al. 19	409	
	Halperin, Oliver, and Stoughton ²⁰	120 ± 12	1060 ± 110
	Benjamin, MacMurdo, and Spencer ¹⁴	82 ± 5	778 ± 50
	Zhuravlev, Kroshkin, and Chetreikov ²¹	80 ± 7	730 ± 70
	This Experiment	106 ± 53	890 ± 53
²⁵⁰ Cf	Metta et al. ²²	<350	
	This Experiment	112 ± 99	161 ± 39

^{*}The resonance integral is calculated as

$$I_f = \int_{0.5 \text{ eV}}^{80 \text{ keV}} \sigma(E) \frac{dE}{E} ;$$

the resonance integral for ²⁵⁰Cf was calculated as

$$I_f = \int_{0.1 \text{ eV}}^{80 \text{ keV}} \sigma(E) \frac{dE}{E} .$$

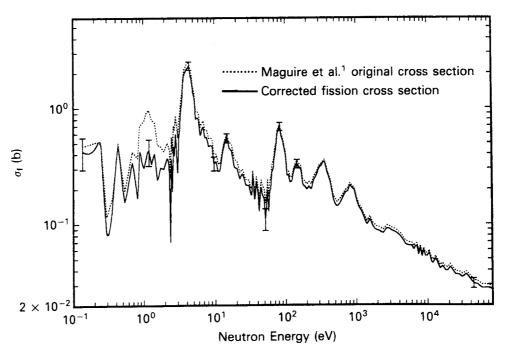


Fig. 5. The ²⁴⁶Cm fission cross section corrected for ²⁴⁷Cm impurities.

smaller than that which we calculated. With a small level spacing and no resonances below ~2 eV, the RINS system will not resolve any resonances, and all we could expect to see is a smooth cross section with some small wiggles due to structure. The other possibility is that ²⁵⁴Es has large fission widths, larger than the level spacing; therefore, resonances overlap each other, and the continuum we see is the true structure of the ²⁵⁴Es fission cross section. The answer to this problem can be found only by performing another experiment with better resolution.

The 254 Es fission cross section was extrapolated to 0.025 eV, and the thermal cross section was found to be 1749 ± 110 b. Table IV lists some other values of thermal cross sections for 254 Es. Our value is in good agreement with the Halperin et al. 17 value of 1970 ± 200 b. Our resonance integral was found to be 896 ± 54 b, which is lower than the Halperin et al. value of 1200 ± 250 and lower than MacMurdo and Harbour, 16 who measured 2200 ± 90 . The 6% error in the resonance integral is mainly the result of uncertainties in flux normalization, counting efficiency, and sample mass.

IV.C. Californium-250

The 250 Cf sample was the smallest sample we had in this experiment, only $0.149 \pm 0.008 \,\mu g$. This sample also had the highest spontaneous fission rate of 442 ± 11 spontaneous fission/s. The signal-to-background ratio is very close to zero in most energy regions, but still we were able to see a single resolved resonance at

0.53 eV with a peak cross section of 184 ± 35 b and an area of 71 ± 9 b·eV and some structure in the energy range of 17 to 76 eV with an average cross section of ~ 4 b. The cross section multiplied by \sqrt{E} is plotted in Fig. 4 and given in Table II. This result shows the advantage of using a lead slowing-down-time spectrometer to obtain high flux for such measurements. The fission cross section of 250 Cf was averaged in the energy range from 1.5 to 61 eV, and assuming a 1/v cross section, we extrapolated to 0.025 eV and calculated a contribution to the thermal cross section of 112 ± 99 b. We found only one other measurement by Metta et al. 22 that reported the cross section to be <350 b.

V. CONCLUSIONS

The fission cross sections of ²⁵⁴Es and ²⁵⁰Cf were first measured in the energy range of 0.1 eV to 80 keV. Einsteinium-254 showed only very little structure possibly because of wide fission widths and small level spacing; only further experiments with better resolution can verify that. The ²⁵⁰Cf fission cross section has only one resonance at 0.53 eV and has an average cross section of the order of ~4 b in the 17- to 76-eV energy range.

This is the first ²⁴⁷Cm fission cross-section measurement at the energy range of 0.1 to 20 eV, and the resonance parameters obtained are in good agreement with those from the Belanova et al. transmission measurement and Mughabghab's evaluation. In the energy range from 20 eV to 100 keV, the shape of the cross

section agrees with the fission cross section measured by Moore and Keyworth, but >150 eV, our results are ~30% higher. Thermal cross sections were extrapolated for ²⁵⁴Es and ²⁴⁷Cm, and they are in good agreement with other experimental results; in the case of the ²⁵⁰Cf thermal cross section, there is no other measurement with which to compare.

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